Fuzzy Logic Controller for Sensorless Direct Torque Control of an Induction Motor Driven by a Matrix Converter

El Mehdi Chiali*, Ahmed Massoum†, Salah Hanafi‡ and Nabil Taib§

1ICEPS Laboratory (Intelligent Control & Electrical Power Systems), Djillali Liabes University of Sidi Bel-Abbes, Sidi Bel-Abbes, Algeria, E-mail:
2L.T.I.I. Laboratory, University of Bejaia, Bejaia 06000, Algeria

Received 4 May 2015; Accepted 26 October 2015

Abstract

The direct torque control has become one of the control techniques used for high performances. The major drawback of this strategy is its high torque ripples. This paper proposes the use of matrix converter to reduce the electromagnetic torque ripples, by suitably selecting switching configuration. This switching strategy combines the advantages of matrix converter with the advantages of direct torque control technique, using a fuzzy speed controller and MRAS speed estimator. A speed controller is designed according to the concept of fuzzy logic, to provide a good robustness to the variations of mechanical parameters. A MRAS speed estimator is also used in order to avoid the implementation of an incremental encoder. The obtained results with Matlab-Simulink show the effectiveness of the proposed system.

Keywords: Induction Motor, Direct Torque Control (DTC), Fuzzy Logic Controller (FLC), Matrix Converter (MC), Model Reference Adaptive (MRAS).

1. Introduction

Due to their ease of manufacture and maintenance, induction motors are widely used in industry. Currently, many industrial applications require speed control, position and torque. However a three-phase power system does not allow these commands, because of its constant amplitude and frequency. To this end, the use of power converter is necessary.

Three phase matrix converter has received considerable attention in recent years. Some advantages of the matrix converter can be seen as following: the use of a compact voltage source, providing sinusoidal voltage with varying amplitude and frequency besides the sinusoidal input current and unity input power factor at power supply side.

A matrix converter has a simple topology and a compact design due to the lack of dc-link capacitor for energy storage[1]. It is able to connect each input phase to each output phase via nine bidirectional switches Fig. 1 [2].

Various methods for controlling the matrix converter have been proposed such as the modulation of scalar, also called modulation Venturini[3, 4] or space Vector modulation the most widely used [1, 5].

The strategy of direct torque control (DTC) allows a decoupled control of flux and torque to obtain the performance of a DC machine with separate excitation[6]. The main advantages of DTC are robust and fast torque response, no requirements for coordinate transformation, no requirements for PWM pulse generation and current regulators [7]. The switching can be fixed with applying a modulated hysteresis as proposed in [8].

In this paper a control technique for matrix converter generate, under unity input power factor conditions, voltage vectors needed to control the torque and flux of induction motors. This technique of DTC with matrix converter has already been proposed in several articles[3, 9, 10] but without speed regulation loop which is very important in industry.

Switches are characterized by equation (1):

\[
\begin{align*}
S_{aA} + S_{bA} + S_{cA} &= 1 \\
S_{aB} + S_{bB} + S_{cB} &= 1 \\
S_{aC} + S_{bC} + S_{cC} &= 1
\end{align*}
\]

\[S_{ij} = \begin{cases} 
0 & \text{if switch } S_{ij} \text{ is open} \\
1 & \text{if switch } S_{ij} \text{ is closed}
\end{cases} \]

Fig. 1 Matrix converter.
2. Direct Torque Control with Matrix Converter

2.1. Basic DTC Principles

Several research works have been published on the principle of the DTC [6, 11].

The DTC model is developed in the fixed coordinate system connected to the stator (α, β), we can write equations of voltage $V_S$ and stator flux $\phi_S$ respectively:

$$V_S = R_S I_S + \frac{d\phi_S}{dt}$$  \hspace{1cm} (2)

$$\phi_S(t) = \int (V_S - R_S I_S) dt$$  \hspace{1cm} (3)

The expression of electromagnetic torque can be written as:

$$C_e = \frac{1}{2} P (\bar{\phi}_S \times \bar{T})$$  \hspace{1cm} (4)

The mechanical equation of the induction machine can be written as follows:

$$\dot{J} \Omega_r = C_e - C_r f_r \Omega_r$$  \hspace{1cm} (5)

2.2. Principles of DTC Using Matrix Converter

The matrix converter generates a higher number of output voltage vectors with respect to voltage source inverter (VSI).

As there are always two voltage vectors which may be chosen for one given combination of flux and torque this gives the possibility to control the average value of the sine of the displacement angle between the input line-to-neutral voltage vector and the corresponding input line current vector.

A mathematical model of the MC can be derived from Fig. 1 as follows:

$$\begin{bmatrix} V_{AN} \\ V_{BN} \\ V_{CN} \end{bmatrix} = \begin{bmatrix} S_aA & S_bA & S_cA \\ S_aB & S_bB & S_cB \\ S_aC & S_bC & S_cC \end{bmatrix} \begin{bmatrix} V_{AN} \\ V_{BN} \\ V_{CN} \end{bmatrix}$$  \hspace{1cm} (6)

$$\begin{bmatrix} I_{AN} \\ I_{BN} \\ I_{CN} \end{bmatrix} = \begin{bmatrix} S_aA & S_bA & S_cA \\ S_aB & S_bB & S_cB \\ S_aC & S_bC & S_cC \end{bmatrix} \begin{bmatrix} I_{AN} \\ I_{BN} \\ I_{CN} \end{bmatrix}$$  \hspace{1cm} (7)

From equation (1), 27 possible configurations of switching are obtained, among them only 18 vectors can be used ($\pm 1, \pm 2, ..., \pm 9$) when two outputs are connected to the same input. These vectors are distributed on 6 directions as shown in Fig. 3.

![Fig. 2. Principle of DTC with a matrix converter.](image)

![Fig. 3. Vector diagrams](image)
Assuming that \( V_s \) is the output voltage vector selected by the DTC classic algorithm, from Fig. 3, it is clear that one of the switching states \( \pm 4, \pm 5 \) or \( \pm 6 \) must be selected.

Given that the magnitude and direction of these vectors depends on the input phase voltage vector, only those with the same direction of \( V_s \) and the maximum magnitude will be considered. If the voltage vectors are single in sector 6, the switching state \(-4\) and \(+5\) can be chosen.

If an increase in the power factor is necessary, the average value of \( \sin(\omega) \) must be reduced, the switching state \(-4\) must be selected. On the other hand, if a decrease in the power factor is required, the average value of \( \sin(\omega) \) must be increased, the switching state \(+5\) must be selected. [9] This technique is shown in Table 2.

### Table 2 The switching table for DTC with matrix converter

<table>
<thead>
<tr>
<th>Sector in which the vector is input</th>
<th>( V_1 )</th>
<th>( V_2 )</th>
<th>( V_3 )</th>
<th>( V_4 )</th>
<th>( V_5 )</th>
<th>( V_6 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( +1 )</td>
<td>-3</td>
<td>+9</td>
<td>-6</td>
<td>+3</td>
<td>-9</td>
<td>+6</td>
</tr>
<tr>
<td>( -1 )</td>
<td>+1</td>
<td>-7</td>
<td>+4</td>
<td>-1</td>
<td>+7</td>
<td>-4</td>
</tr>
<tr>
<td>( +2 )</td>
<td>-8</td>
<td>+5</td>
<td>-2</td>
<td>+5</td>
<td>-5</td>
<td></td>
</tr>
<tr>
<td>( -1 )</td>
<td>+2</td>
<td>-8</td>
<td>+5</td>
<td>-2</td>
<td>+8</td>
<td>-5</td>
</tr>
<tr>
<td>( +3 )</td>
<td>-1</td>
<td>+7</td>
<td>-4</td>
<td>+1</td>
<td>-7</td>
<td>+4</td>
</tr>
<tr>
<td>( -1 )</td>
<td>+3</td>
<td>-9</td>
<td>+6</td>
<td>-9</td>
<td>+6</td>
<td></td>
</tr>
<tr>
<td>( +4 )</td>
<td>-1</td>
<td>+7</td>
<td>-4</td>
<td>+1</td>
<td>-7</td>
<td>+4</td>
</tr>
<tr>
<td>( -1 )</td>
<td>+4</td>
<td>-8</td>
<td>+5</td>
<td>-2</td>
<td>+8</td>
<td>-5</td>
</tr>
<tr>
<td>( +5 )</td>
<td>-2</td>
<td>+8</td>
<td>-5</td>
<td>+2</td>
<td>-8</td>
<td>+5</td>
</tr>
<tr>
<td>( -1 )</td>
<td>+3</td>
<td>-9</td>
<td>+6</td>
<td>-3</td>
<td>+9</td>
<td>-6</td>
</tr>
<tr>
<td>( +6 )</td>
<td>+1</td>
<td>-7</td>
<td>+4</td>
<td>-1</td>
<td>+7</td>
<td>-4</td>
</tr>
<tr>
<td>( -1 )</td>
<td>-2</td>
<td>+8</td>
<td>-5</td>
<td>+2</td>
<td>-8</td>
<td>+5</td>
</tr>
</tbody>
</table>

3. Speed Loop Estimation

For the speed loop, we replaced the incremental encoder by the MRAS estimator from which we obtain the estimated speed from the stator current and voltage induction motor. This technique is used not only to reduce the cost of the system, but also to eliminate the need for additional space for mounting and maintenance of the incremental encoder.

To ensure the speed control, we used a fuzzy controller which is insensitive to machine parameter variation and also in order to reduce the response time for speed.

3.1. Model Reference Adaptive System

The MRAS (model reference adaptive system) is based on comparing the outputs of two estimators. The first, which does not introduce the quantity to estimate (the speed in this case) is called the reference model and the second is the adjustable model [12].

PL regulator has the role of an adaptation mechanism to generate the estimated speed, as shown in Fig. 4.

3.2. Five Rules Fuzzy Logic Controller

FLC requires some arbitrary decisions concerning rule base, input and output membership functions. This makes the design procedure strongly dependent on expert knowledge [13]. Fig. 5 shows the schematic model of FLC based speed regulator.

### Table 3. Fuzzy control rules

<table>
<thead>
<tr>
<th>( \Delta e )</th>
<th>NL</th>
<th>NS</th>
<th>ZE</th>
<th>PS</th>
<th>PL</th>
</tr>
</thead>
<tbody>
<tr>
<td>NL</td>
<td>NL</td>
<td>NL</td>
<td>NL</td>
<td>NS</td>
<td>ZE</td>
</tr>
<tr>
<td>NS</td>
<td>NL</td>
<td>NL</td>
<td>NL</td>
<td>NS</td>
<td>ZE</td>
</tr>
<tr>
<td>ZE</td>
<td>NL</td>
<td>NS</td>
<td>ZE</td>
<td>PS</td>
<td>PL</td>
</tr>
<tr>
<td>PS</td>
<td>NS</td>
<td>ZE</td>
<td>PS</td>
<td>PL</td>
<td>PL</td>
</tr>
<tr>
<td>PL</td>
<td>ZE</td>
<td>PS</td>
<td>PL</td>
<td>PL</td>
<td>PL</td>
</tr>
</tbody>
</table>

The model is presented as follows:

\[
e = w_r^{ref} - w_r^{ef} \quad \text{and} \quad \Delta e(k) = e(k) - e(k - 1)
\]

Where \( w_r^{ref} \) is the reference speed and \( w_r \) is the actual speed of rotor, \( e(k) \) is the error and \( \Delta e(k) \) is the error change. Then the output variable of the FLC is presented by the reference torque control \( C_{r,ref} \).

7. Simulation Results and Interpretation

The whole system has been simulated using the Matlab-Simulink package. The machine used for simulation is a three-phase 1.5 kW induction motor with the following parameters shown in Table 4.

### Table 4. Induction Motor Parameters

<table>
<thead>
<tr>
<th>( P )</th>
<th>1.5 kW</th>
<th>( R_r )</th>
<th>3.81 ( \Omega )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( U )</td>
<td>380 v</td>
<td>( L_s, L_r )</td>
<td>0.274 H</td>
</tr>
<tr>
<td>( N )</td>
<td>1450 tr/min</td>
<td>( M )</td>
<td>0.258 H</td>
</tr>
<tr>
<td>( P )</td>
<td>2</td>
<td>( J )</td>
<td>0.031 kgm²</td>
</tr>
<tr>
<td>( R_s )</td>
<td>4.85 ( \Omega )</td>
<td>( f_r )</td>
<td>0.0114 Nm/rd/s</td>
</tr>
</tbody>
</table>
Figure 6 shows a good performance in terms of stator current, stator flux and electromagnetic torque. As it can be seen, stator current shows a sinusoidal waveform, while the stator flux and torque are following their references.

In the transitional regime, the flux variations are faster than those of the torque, and when they reach the steady state, the torque and flux are limited by the hysteresis comparators. It should be noted that the torque follows the new setpoint very quickly. The results of simulation show that the FLC
gives better responses compared to a conventional PI controller. The time response speed is very good without overshoot. Moreover, the corresponding values are represented in Table 5.

<table>
<thead>
<tr>
<th>Controller Type</th>
<th>Settling Time (ms)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PI Controller</td>
<td>200 ms</td>
</tr>
<tr>
<td></td>
<td>600 ms (response to load torque)</td>
</tr>
<tr>
<td>FLC</td>
<td>144 ms</td>
</tr>
<tr>
<td></td>
<td>40 ms (response to load torque)</td>
</tr>
</tbody>
</table>

Knowing that the speed response given by the MRAS estimator is almost the same to the actual speed. The only major drawback is that the matrix converter output voltage is limited to 86.6% of the input voltage.

8. Conclusion

The basic idea of the work presented is the performances analysis of the DTC applied to induction machine fed by matrix converter. The speed regulation loop contains both of a speed MRAS estimator and FLC regulator. The direct torque control of an induction machine provides a satisfactory solution to electric drives problems in terms of robustness and dynamics encountered in control techniques based on the orientation of the rotor flux using voltage source inverters. The use of matrix converter allowed an improvement in the DTC performances aiming to reduce torque oscillations because of the best quality of the input and output waveforms provided. In addition, FLC regulator proves its good performance for speed regulation of induction motor shown by the obtained results. This latter, gives an added value to the electrical machine drive. Moreover, the MRAS based speed estimator allows reduced cost and size of the control system. The advantages provided by the proposed system make it competitive with regard to the other proposed solutions.

References

2. F.Gruson , Modulation naturelle générale des convertisseurs matriciels pour la variation de vitesse, PRES-Université Lille Nord de France 13 décembre 2010.
13. F.Daya.JL, V.Subbiah, A Novel Fuzzy Logic Based Robust Speed Controller for Permanent Magnet Synchronous Motor Servo Drive, 2009

Appendix

$R_S, R_F$: Stator and rotor inductance.
$L_S$: Stator inductance.
$M$: Mutual inductance.
$T_F$: Rotor time constant.
$C_E$: Electromagnetic torque.
$C_F$: Resistive torque.

$\varphi_S$: Stator flux.
$P$: Pole pairs.
$J$: Moment of inertia.
$\Omega_F$: Rotor speed.
$\omega_F$: Rotor angular frequency.